# A TEST-BED FOR LINEAR TIME, CONSTANT SPACE DIFFERENCING ALGORITHMS 

## By

Pauline Mouawad

A Thesis

Submitted in Partial Fulfillment of the Requirements for the Degree of Master of Science in Computer Science

Department of Computer Science Faculty of Natural and Applied Sciences

Notre Dame University - Louaize

Zouk Mosbeh, Lebanon

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"Let us, then, be up and doing, with a heart for any fate; still achieving, still pursuing, learn

to labor and to wait."<br>Henry Wadsworth Longfellow

If one finds passion in one's work, how can this merriment be full if it has no gratitude to show? I cannot be content with a work that is merely the fruit of a singular root but rather, I draw satisfaction from the knowledge that ultimately, I have someone to thank.

My thanks are due to my parents and my sister, for always being there for me. Their encouragement and support have been most precious to the fulfillment of this achievement. I couldn't have done this without them.

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My deepest respect and gratitude to Notre Dame University, that gave me the education and knowledge I sought. I also owe a well of gratitude to the teachers who have taught me throughout the graduate study; they truly made this possible. I dedicate this thesis to my family and loyal friends; they really make the world a nicer place to live in.


#### Abstract

This thesis is motivated by the latest work related to Differential compression algorithms as it appears in the work of Ajtai, et al. - 2002. In particular, we pay special attention to delta encoding algorithms that achieve good compression in linear time and constant space. This is important because previous work in this area uses either quadratic time and constant space or linear time and linear space, which is unacceptable for large inputs. In delta encoding, the algorithm reads two different copies of the same file as input, termed the reference copy and the version copy. The output of the algorithm is a sequence of Add/Copy commands that reconstructs the version copy in the presence of the reference copy. Such algorithms have been recommended to be integrated into the http protocol. The idea is to reduce the data transfer time for text and http objects in order to decrease the latency of loading updated web pages. Also, in a client server system, clients may perform delta encoding to exchange delta encodings with a server instead of exchanging whole files. This reduces the time needed to perform the backup and reduces the storage required at the backup server. In the literature, the evaluation of delta encoding algorithms depends on three metrics: the running time of the algorithm, the space it uses, and the compression results it achieves. In this thesis we build a test-bed for delta encoding algorithms that accommodates most of the previous work described in the literature. Through intensive experimentations we are able to recommend a hybrid algorithm that forms a good compromise among the existing methods.


## TABLE OF CONTENTS

List of Figures ..... vi
List of Tables ..... vii
I The Problem ..... 1
II Literature Review ..... 4
2.1 Delta Encoding Compression Technique ..... 5
2.2 Notations ..... 7
2.3 Outline of the Algorithm ..... 9
III A Test-Bed ..... 21
3.1 The Algorithm ..... 22
3.2 Time and Space Complexity ..... 25
IV Experimental Results ..... 27
4.1 Tables and Graphs ..... 27
4.2 Recommendations ..... 39
V Conclusion ..... 41
VI References ..... 42
VII Appendix ..... 44

## LIST OF FIGURES

Figure
2.1 Pseudocode for the Greedy algorithm ..... 11,12
2.2 Pseudocode for the One-Pass algorithm ..... 13, 14
2.3 Pseudocode for the Correcting One-Pass algorithm ..... $15,16,17$
2.4 Pseudocode for the Correcting 1.5-Pass algorithm ..... 18,19
3.1 Pseudocode for the Test-Bed algorithm ..... 23, 24
4.1 Average Cost Graph - Files of Size 1K ..... 29
4.2 Average Cost Graph - Files of Size 8K ..... 31
4.3 Average Cost Graph - Files of Size 30K ..... 33
4.4 Average Cost Graph - Files of Size 40K ..... 35
4.5 Average Cost Graph - Files of Size 70K ..... 37
4.6 Average Cost Graph - Files of Size 100K ..... 39

## LIST OF TABLES

## Table

4.1.1.1 Average Values. $\mathrm{P}=1.1 \mathrm{~K}$ files ..... 28
4.1.1.2 Average Values. $\mathrm{P}=2.1 \mathrm{~K}$ files ..... 28
4.1.1.3 Average Values. $\mathrm{P}=3.1 \mathrm{~K}$ files ..... 28
4.1.1.4 Average Values. $\mathrm{P}=8.1 \mathrm{~K}$ files ..... 28
4.1.1.5 Average Values. $\mathrm{P}=16.1 \mathrm{~K}$ files ..... 28
4.1.2.1 Average Values. $\mathrm{P}=1.8 \mathrm{~K}$ files ..... 29
4.1.2.2 Average Values. $\mathrm{P}=2.8 \mathrm{~K}$ files ..... 29
4.1.2.3 Average Values. $\mathrm{P}=3.8 \mathrm{~K}$ files ..... 30
4.1.2.4 Average Values. $\mathrm{P}=8.8 \mathrm{~K}$ files ..... 30
4.1.2.5 Average Values. $\mathrm{P}=16.8 \mathrm{~K}$ files ..... 30
4.1.3.1 Average Values. $\mathrm{P}=1.30 \mathrm{~K}$ files ..... 31
4.1.3.2 Average Values. $\mathrm{P}=2.30 \mathrm{~K}$ files ..... 31
4.1.3.3 Average Values. $\mathrm{P}=3.30 \mathrm{~K}$ files ..... 32
4.1.3.4 Average Values. $\mathrm{P}=8.30 \mathrm{~K}$ files ..... 32
4.1.3.5 Average Values. $\mathrm{P}=16.30 \mathrm{~K}$ files ..... 32
4.1.4.1 Average Values. $\mathrm{P}=1.40 \mathrm{~K}$ files ..... 33
4.1.4.2 Average Values. $\mathrm{P}=2.40 \mathrm{~K}$ files ..... 33
4.1.4.3 Average Values. $\mathrm{P}=3.40 \mathrm{~K}$ files ..... 34
4.1.4.4 Average Values. $\mathrm{P}=8.40 \mathrm{~K}$ files ..... 34
4.1.4.5 Average Values. $\mathrm{P}=16.40 \mathrm{~K}$ files ..... 34
4.1.5.1 Average Values. $\mathrm{P}=1.70 \mathrm{~K}$ files ..... 35
4.1.5.2 Average Values. $\mathrm{P}=2.70 \mathrm{~K}$ files ..... 35
4.1.5.3 Average Values. $\mathrm{P}=3.70 \mathrm{~K}$ files ..... 36
4.1.5.4 Average Values. $\mathrm{P}=8.70 \mathrm{~K}$ files ..... 36
4.1.5.5 Average Values. $\mathrm{P}=16.70 \mathrm{~K}$ files ..... 36
4.1.6.1 Average Values. $\mathrm{P}=1.100 \mathrm{~K}$ files ..... 37
4.1.6.2 Average Values. $\mathrm{P}=2.100 \mathrm{~K}$ files ..... 37
4.1.6.3 Average Values. $\mathrm{P}=3.100 \mathrm{~K}$ files ..... 38
4.1.6.4 Average Values. $\mathrm{P}=8.100 \mathrm{~K}$ files ..... 38
4.1.6.5 Average Values. $\mathrm{P}=16.100 \mathrm{~K}$ files ..... 38

## CHAPTER I

## The Problem

During the last decade, the field of computer science has witnessed a widespread development that grew significantly. This growth triggered an increase in the demand for fast data transmission over the network (Internet or intranet). The solution was to compress large files into smaller versions so that they can be managed easily. Various techniques have been suggested and consequently provided solutions to the problem. Unfortunately limitations were encountered because no matter what the technique is, compressed files are still too large for a remote transmission and still require enormous transfer time and create unacceptable traffic over the network. Concisely, time and space are still a major issue to be dealt with.

Recent studies have used differential compression techniques in an attempt to solve the problem and various algorithms have been proposed $[1,3,4,6,7,8,9]$. The main concept is to try to find common strings between two versions of data and use them to encode one version compactly; this is accomplished by describing the encoding itself as a set of changes of one version with respect to its companion. Instead of compressing a whole new file to replace wholly an older version of it, we would rather check for the changes in it and generate some code that would only send those changes to the older version. A simple process ultimately combines the file with the changes. This is quite an interesting approach because it considerably cuts the size of the file to be compressed.

Recently, new algorithms have been put that run in linear time and use constant space. But the tradeoff is with the compression results. The algorithm has to disregard some strings in the file in favor of its running time and space usage. And sometimes a significant portion in the file is not encoded because the algorithms favor the recent scanned strings over the previously read ones and therefore information about past strings is completely lost. More on this will be described in the next chapter.

This thesis introduces a new algorithm, which attempts to yield near to optimal results by checking almost every string of length $p$ in both files: the old one called Reference and the new one called Version. Similarities found are encoded with a Copy command from the Reference while non-matching strings are encoded with an Add command from the Version. The method used ensures a window into the past of the files being scanned in a sense that it examines almost all strings and it does not favor a string over the other except for strings that yield longer matches. We keep in mind that one string may match differently depending on how long it can extend in the file and still matches its copy in the other file. For example, a string of length $p=3$ consisting of $a b c$ in the Reference file that only matches to $a b c$ in the Version file is far less beneficial than the same string $a b c$ that extends in both the Reference and Version files to become abcdefghijklmnop of length $p=16$. Therefore this considerably diminishes the amount of strings left un-encoded. Moreover, instead of having several copy commands to encode a string of length $\mathrm{p}=16,1$ copy command does so and clearly decreases the cost of the compression. Also and very importantly, this algorithm cuts down on transmission time and on storage space. Ultimately, only variations of the file are being transmitted to the user, which means a major cut down
on Internet transfer time to the user's satisfaction. Finally and at the user-end, the program is run and the file is assembled and becomes the new updated version. The fashion by which the cost of such technique is computed will be described in a later chapter, in full.

The rest of the thesis is organized as follows. Chapter II offers an overview of related algorithms from the literature. Chapter III is our contribution in which we describe a Test-Bed of differencing algorithms that run in linear time and constant space. The actual code is included in the Appendix and heavily commented for a clear and friendly reading. Chapter IV lays down a series of tests conducted on different files of different sizes while varying the size of a specific variable $L$ in the code to be revealed later on. A series of Table and Graph representations will accompany those tests for a concise and obvious conclusion about the Average Cost of our algorithm as well as the time and space complexities. Chapter V is the conclusion.

## CHAPTER II

## Literature Review

Given two strings V and R , differential compression is about encoding $V$ with respect to $R$ by finding regions of $V$ identical to regions of $R$ and encoding this data with a reference to the location and size of the data in $R$ [1]. At each step during execution, the algorithm examines strings, also called seeds, having a constant length p. Generally, the inputs to a differential compression algorithm are strings from both the Reference and Version files, and the output is a delta string:

$$
\Delta(\mathbf{R}: \mathbf{V})=A(\mathbf{R}: \mathbf{V})
$$

The output $\Delta$ will consist of a sequence of commands that will be described in the next section under Delta Encoding.

As mentioned earlier, the performance of this algorithm is measured using three metrics:

1. The time complexity. It is the running time of the algorithm.
2. The space complexity. It is the storage space the algorithm uses in order to process the strings read from both files.
3. The compression results achieved. These are the series of commands issued that differentiate between the similarities and the differences among the two versions of a file. Hence the term differential compression.

The purpose of this type of encoding is to find algorithms that would ultimately, no matter the file sizes or the scale of the input, generate a near to optimal compression result while cutting down on transmission time and storage space.

In this study, all the algorithms discussed follow the Delta Encoding Compression Algorithm which we describe next.

### 2.1 Delta Encoding Compression Technique

Given two copies of a file, the Reference - standing for the old version - and the Version - being the new version - , the delta encoding algorithm is about finding the longest match possible of a given string after performing a left-to-right scan of both files in a parallel fashion in search of matching seeds of an initial length $p$. In the event where such match is found, an attempt to extend that match to a longer one takes place. This is called the extension phase.

When a matching string is located, a command is issued in the form:

$$
(C, l, a)
$$

The character $C$ stands for the command Copy, $l$ stands for the length of the string to be copied, and $a$ stands for the address. This reads into the following: Copy a string of length $l$ found at offset $a$ in the Reference file.

On the other hand, when a non-matching string is encountered, a different command is issued in the form:

$$
(A, l, S)
$$

The character A represents the command Add, lstands for the length of the string to be added, and $S$ is the actual string being added. And it reads: Add a string $S$ of length $l$ from the Version file.

A simple example follows to illustrate this concept:

Given: $\quad R=A B C D E L M N O P Q R S T X Y Z$
\&
$V=F G H I J K L M N O P U V W X Y Z$
A Delta Encoding output would be:
[(A, 4, 'FGHIJK'), (C, 5, '5'), (A, 3, 'UVW'), (C, 3, '14')]

The identification of fixed length matching strings is done by reducing the seed to a fixed integer by means of a hash function $F$. The resulting integer of the form $F(S)$ is called the seed's footprint. Assuming an ideal hashing function, one footprint should uniquely identify a given seed; but such consideration would be misleading since in a real life application, two different seeds might in fact hash to the same footprint value.

The hashing function $F$ generates a hash table with the number of its entries equal to the number of footprints generated. Indeed, a hash table entry is a footprint and a hash table size depends on the number of footprints stored. A hash table entry that corresponds to one or more seeds scanned may hold one or more offsets indicating the respective addresses of those seeds, depending on the algorithm used. Some algorithms do not allow more than one offset to be stored at a given footprint, as we shall see in the coming sections.

### 2.2 Notations

The notations used for differential compression are:

### 2.2.1 - Pointers:

The following pointers are defined in the code:
$\mathrm{v}_{\mathrm{c}}$ : Current address of the Version string
$r_{c}$ : Current address of the Reference string
$v_{s}$ : Starting offset of a version string. This pointer holds the starting offset of the un-encoded suffix of the version string.
$v_{\mathrm{m}}$ : Offset of a matching version string.
$r_{m}$ : Offset of a matching reference string.

### 2.2.2 - Parameters

The following parameters are defined as well:
p: Seed length. It's the length of substrings of which a footprint is calculated.
q : The size of the hash table $=$ the number of footprint values.
$|X|$ : Length of a string $X$
$n=|R|+|V|$ : The combined length of the reference and version strings.

### 2.2.3 - Hashing function

The following hashing function due to Karp and Rabin [1987] is used in the code:

If $\mathrm{x}_{0}, \mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}-1}$ are the symbols of a string $X$ of length $n$, let $X_{r}$ denote the substring of length $p$ starting at offset $r$. Thus,
$X_{r}=\mathrm{x}_{\mathrm{r}} \mathrm{X}_{\mathrm{r}+1} \ldots \mathrm{X}_{\mathrm{r}+\mathrm{p}-1}$.
Identify the symbols with the integers $0,1, \ldots, \mathrm{~b}-1$, where $b$ is the number of symbols. Let $q$ be a prime, the number of footprint values. To compute the modular hash value (footprint) of $X_{r}$, the substring $X_{r}$ is viewed as a base- $b$ integer, and this integer is reduced modulo $q$ to obtain the footprint; that is:

$$
\mathrm{F}_{\mathrm{X}}(\mathrm{a}, \mathrm{a}+\mathrm{p})=\left(\sum_{i=r}^{r+p-1} x_{i} b^{r+p-1-i}\right) \bmod q .
$$

Using this method, a footprint function is specified by two parameters: $p$, the length of substrings (seeds) to which the function is applied; and $q$, the number of footprint values. The choice of $q$ involves a trade-off between space requirements and the extent to which the footprint values of a large number of seeds have different footprints. Typically, a footprint value gives an index into a hash table. The advantage of this function is that footprinting allows an algorithm to detect matching seeds of length $p$, but the algorithms in the literature are most successful when these seeds are part of much longer matching substrings; in this case, a matching seed leads the algorithm to discover a much longer match. The hashing function notations are:
$\mathrm{F}_{\mathrm{X}}(\mathrm{a}, \mathrm{a}+\mathrm{p})$ : The footprint of a seed X , starting at offset ' $a$ ' up to
offset $a+p$ where p is the substring's length.
$\mathrm{H}_{\mathrm{X}}$ : The hash table, indexed by seeds' footprints.
$H_{X}$ [i]: The $i$ th element in hash table $\mathrm{H}_{\mathrm{X}}$. In general, hash table entries
contain the starting offsets of seeds indexed by footprint value.

### 2.3 Outline of the Algorithm

1. Initialize the hash table(s). Create empty hash table(s).
2. Initialize pointers. Set $\mathrm{v}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{s}}$ to zero.
3. Generate new footprints. Generate a new footprint at $\mathrm{v}_{\mathrm{c}}$ and at $\mathrm{r}_{\mathrm{c}}$ if there is enough input string to the right of $v_{c}$ and $r_{c}$ to generate a new footprint. If at least one footprint was generated, continue at Step (4). If not, go to Step (8) to finish the encoding of $V$ and terminate.
4. Try to find a matching seed. Use the newly generated footprint(s) and the hash table(s) to try to find a matching seed in $R$ and $V$. In some algorithms, the new footprint(s) are also used to update the hash tables. If a matching seed is not found, increment $v_{c}$ (and increment $r_{c}$ ) by one, and repeat Step (3). If a matching seed is found, continue at Step (5) to extend the match.
5. Extend the match. Attempt to extend the matching seed to a longer matching substring in both $R$ and $V$ by comparing symbols between $R$ and $V$.
6. Encode the match. Encode the substring of $V$ from $v_{s}$ to the end of the matching substring by producing the appropriate command sequence; this will always end with a copy command that encodes the matching substring. Update $\mathrm{v}_{\mathrm{s}}$ to the new start of the unencoded suffix.
7. Update and return to top of main loop. Update $\mathrm{v}_{\mathrm{c}}\left(\right.$ and $\left.\mathrm{r}_{\mathrm{c}}\right)$ and modify the hash tables if needed. Return to Step (3).
8. Finish up. If there is an unencoded suffix of $V$, encode this suffix with an add command.

### 2.3.1 - A Greedy Differencing Algorithm

This algorithm is based on [9]. The greedy algorithm first makes a pass over the reference string $R$; it computes footprints and stores in a hash table, for each footprint $f$, all offsets in $R$ that have footprint $f$ (colliding footprints are handled by chaining footprints at each value). The algorithm then moves the pointer $\mathrm{v}_{\mathrm{c}}$ through $V$, and computes a footprint at each offset. At each step it does an exhaustive search, using the hash table and the strings $R$ and $V$, to find the longest substring of $V$ starting at $\mathrm{v}_{\mathrm{c}}$ that matches a substring appearing somewhere in $R$. The longest matching substring is encoded as a copy command, $\mathrm{v}_{\mathrm{c}}$ is set to the offset following the matching substring, and the process continues.

The pseudocode in Figure 2.1 outlines the major steps of the greedy algorithm. In Step(1), the algorithm hashes the contents of the reference string in a hash table where each entry is a footprint containing all the offsets having that footprint; in Steps(3) to (6), the algorithm then finds longest matching substrings in the version string and encodes them.

Obviously, the space used by this algorithm is dominated by the space for the hash table $(=|R|-p+1$ offset values stored in linked lists). Since $p$ is a constant, the space is proportional to $|\mathrm{R}|$. Concerning the bound of the time complexity, at each offset in R , the algorithm spends $\mathrm{O}(l)$ time, in the worst case, to find a matching substring of length at most $l$ starting at this offset. Thus, the total time is $\mathrm{O}(|\mathrm{V} \| \mathrm{R}|)$,
that is, $\mathrm{O}\left(\mathrm{n}^{2}\right)$. It is known in [1] that the greedy algorithm provides a solution to the perfect differencing problem if $\mathrm{p} \leq 2$. The pseudocode that follows represents the basic steps executed by the greedy differencing algorithm.

Given a reference string R and a version string V , generate a delta encoding of V as follows:

1. For all offsets in input string $R$ in the interval $[0,|R|-p]$, generate the footprints
2. Start string pointers $\mathrm{v}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{s}}$ at offset zero in $V$.
3. If $\mathrm{v}_{\mathrm{c}}+\mathrm{p}>|\mathrm{V}|$ go to Step (8). Otherwise, generate a footprint $F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ at $v_{c}$.
4. (and (5)) In this algorithm it is natural to combine the seed matching and substring extension steps into one step. Examine all entries in the linked list at $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$ (this list contains the offsets in $R$ that have footprint $F_{V}\left(\mathrm{v}_{\mathrm{c}}\right.$, $\left.\mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ ) to find an offset $\mathrm{r}_{\mathrm{m}}$ in $R$ that maximizes $l$, where $l$ is the length of the longest matching substring starting at $\mathrm{r}_{\mathrm{m}}$ in $R$ and at $\mathrm{v}_{\mathrm{c}}$ in $V$. If no substring starting at the offsets listed in $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$ matches a substring starting at $v_{c}$, increment $v_{c}$ by one and return to Step (3). Otherwise, set $v_{m}$ and $r_{m}$ to the start offsets of the longest matching substring found. (In this algorithm, $\mathrm{v}_{\mathrm{m}}=\mathrm{v}_{\mathrm{c}}$ at this point.) Let $l$ be the length of this longest matching substring.
5. The longest match extension has already been done in the combined step above.
6. If $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right)$ using an add command containing the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right)$ to be added. Encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ as a copy of the substring of length $l$ starting at offset $\mathrm{r}_{\mathrm{m}}$ in $R$. Set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
7. Set $\mathrm{v}_{\mathrm{c}}$ to $\mathrm{v}_{\mathrm{m}}+l$ and return to Step(3)
8. All of the remaining unencoded input has been processed with no matching substrings found. If $\mathrm{v}_{\mathrm{s}}<|\mathrm{V}|$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}},|\mathrm{V}|\right)$ with an add command. Terminate the algorithm.

Figure 2.1 Pseudocode for the greedy algorithm

### 2.3.2 - The One-Pass Algorithm

The one-pass differencing algorithm finds a delta encoding in linear time and constant space. It finds matching substrings in a next match sense. That is, after copy-encoding a matching substring, the algorithm looks for the next matching substring forward in both input strings and disregards the portion of R and V that precedes the end of the substring that has just been copy-encoded. Hence it has a linear time complexity. The one-pass algorithm does not store all offsets having a certain footprint; instead it stores, for each footprint, at most one offset in R and at most one in V . This makes the hash table for R smaller with a size q rather than $|\mathrm{R}|$ and more easily searched however the compression is not always optimal. This algorithm works in a first-fit fashion, which means that it retains only the first offset found after each flush of the hash table. Hence it uses O (q) space. The drawback though, is that in the presence of transposed data (with R as ... X ... Y and V as ... Y ... X ...), the algorithm will not detect both of the matching substrings X and Y . Pseudocode of the one-pass algorithm follows.

Given a reference string $R$ and a version string $V$, generate a delta encoding of $V$ as follows:
(1) Create empty hash tables, $H_{V}$ and $H_{R}$, for $V$ and $R$. Initially, all entries are empty.
(2) Start pointers $r_{c}, v_{c}$, and $v_{s}$ at offset zero. Pointer $v_{s}$ marks the start of the suffix of $V$ that has not been encoded.
(3) If $\mathrm{v}_{\mathrm{c}}+\mathrm{p}>|\mathrm{V}|$ and $\mathrm{r}_{\mathrm{c}}+\mathrm{p}>|\mathrm{R}|$ go to Step (8). Otherwise, generate footprint $F_{V}$ $\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{v}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{V}|$ and footprint $F_{R}\left(\mathrm{r}_{\mathrm{c},} \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{r}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{R}|$.
(4) For footprints $F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ and $F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ :
(a) Place the offset $\mathrm{v}_{\mathrm{c}}$ (resp., $\mathrm{r}_{\mathrm{c}}$ ) into $H_{V}$ (resp., $H_{R}$ ), provided that no previous entry exists. The hash tables are indexed by footprint. That is, if $H_{V}$ $\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]=$ empty assign $\mathrm{v}_{\mathrm{c}}$ to $H_{V}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$; similarly, if $H_{R}\left[F_{R}\right.$ $\left.\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]=$ empty, assign $\mathrm{r}_{\mathrm{c}}$ to $H_{R}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$.
(b) If there is a hash table entry at the footprint value in the other string's hash table, the algorithm has found a likely matching substring. For example, $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty indicates a likely match between the seed at offset $\mathrm{r}_{\mathrm{c}}$ in $R$ and the seed at offset $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ in $V$. In this case set $\mathrm{r}_{\mathrm{m}}$ to $\mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{m}}$ to $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ to the start offsets of the potential match. Check whether the seeds at offsets $r_{m}$ and $v_{m}$ are identical. If the seeds prove to be the same, matching substrings have been found. If this is the case, continue at Step (5) to extend the match (skipping the rest of Step (4b)). Symmetrically, if $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}\right.\right.$, $\left.\left.\mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty, set $\mathrm{v}_{\mathrm{m}}$ to $\mathrm{v}_{\mathrm{c}}$ and $\mathrm{r}_{\mathrm{m}}$ to $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$. If the seeds at offsets $\mathrm{r}_{\mathrm{m}}$ and $v_{m}$ are identical, continue at Step (5) to extend the match. At this point, no
match starting at $v_{c}$ or starting at $r_{c}$ has been found. Increment both $r_{c}$ and $v_{c}$ by one, and continue hashing at Step (3).
(5) At this step, the algorithm has found a matching seed at offsets $v_{m}$ and $r_{m}$. The algorithm matches symbols forward in both strings, starting at the matching seed, to find the longest matching substring starting at $\mathrm{v}_{\mathrm{m}}$ and $\mathrm{r}_{\mathrm{m}}$. Let $l$ be the length of this substring.
(6) If $v_{s}<v_{m}$, encode the substring $V\left[v_{s}, v_{m}\right)$ using an add command containing the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right)$ to be added. Encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ as a copy of the substring of length $l$ starting at offset $\mathrm{r}_{\mathrm{m}}$ in $R$. Set $\mathrm{v}_{\mathrm{s}}$ to the offset following the end of the matching substring, that is, $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
(7) Set $\mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{c}}$ to the offset following the end of the match in $R$ and $V$, that is, set $\mathrm{r}_{\mathrm{c}}$ to $\mathrm{r}_{\mathrm{m}}+l$. Flush the hash tables by setting all entries to empty. We use a nondecreasing counter (version number) with each hash entry to invalidate hash entries logically. This effectively removes information about the strings previous to the new current offsets $v_{c}$ and $r_{c}$. Return to hashing again at Step (3).
(8) All inputs have been processed. If $v_{s}<|V|$, output an add command for substring $V\left[\mathrm{v}_{\mathrm{s}},|\mathrm{V}|\right)$. Terminate the algorithm.

Figure 2.2 Pseudocode for the one-pass algorithm

### 2.3.3 - The Correcting One-Pass Algorithm

The correcting one-pass algorithm differs from the one-pass algorithm by:
(1) keeping all existing entries in the hash table tables after encoding a copy command; and
(2) discarding a prior offset that has a particular footprint in favor of the current offset having that footprint.

By retaining all entries in the hash table, the correcting one-pass retains information about past substrings i.e. retains a window into the past which enables it to detect nonsequential matching substrings, that is, substrings that occur in the version string in an order different from the order in which they occur in the reference string. The correcting one-pass algorithm extends matching strings both backwards and forwards. This ability of reverse matching permits the correction of early bad encodings and therefore an Add command of a string of length $p=10$ with a cost equal to 10 , can be corrected to one Copy command with a cost equal to 1 in the best case. Despite the similarity between the correcting one-pass algorithm and the onepass algorithm, the correcting one-pass algorithm does not have the same linear running time guarantee. The algorithm spends a large amount of time extending matches backwards at many executions, so that the total time spent during backwards matching grows faster than linearly in the length of the input.

The correcting one-pass algorithm pseudocode is:
Given a reference string $R$ and a version string $V$, generate a delta encoding of $V$ as follows:
(1) Create empty hash tables, $H_{V}$ and $H_{R}$, for $V$ and $R$.
(2) Start pointers $r_{c}, v_{c}$, and $v_{s}$ at offset zero. Pointer $v_{s}$ marks the start of the suffix of $V$ that has not been encoded.
(3) If $\mathrm{v}_{\mathrm{c}}+\mathrm{p}>|\mathrm{V}|$ and $\mathrm{r}_{\mathrm{c}}+\mathrm{p}>|\mathrm{R}|$ go to Step (8). Otherwise, generate footprint $F_{V}$ $\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{v}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{V}|$ and footprint $F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{r}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{R}|$.
(4) For footprints $F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ and $F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ :
(a) Place the offset $\mathrm{v}_{\mathrm{c}}\left(\right.$ resp., $\left.\mathrm{r}_{\mathrm{c}}\right)$ into $H_{V}\left(\right.$ resp., $\left.H_{R}\right)$. That is, assign $H_{V}$ $\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$ to $\mathrm{v}_{\mathrm{c}}$ and $H_{R}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ to $\mathrm{r}_{\mathrm{c}}$.
(b) As in the one-pass algorithm, if $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty, set $\mathrm{r}_{\mathrm{m}}$ to $\mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{m}}$ to $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ to the start offsets of the potential match. If the seeds at offsets $\mathrm{r}_{\mathrm{m}}$ and $\mathrm{v}_{\mathrm{m}}$ are identical, continue at Step (5) to extend the match (skipping the rest of Step (4b)). Symmetrically, if $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty, set $\mathrm{v}_{\mathrm{m}}$ to $\mathrm{v}_{\mathrm{c}}$ and $\mathrm{r}_{\mathrm{m}}$ to $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$. If the seeds at offsets $\mathrm{r}_{\mathrm{m}}$ and $\mathrm{v}_{\mathrm{m}}$ are identical, continue at Step (5) to extend the match. At this point, no match starting at $\mathrm{v}_{\mathrm{c}}$ or starting at $r_{c}$ has been found. Increment both $r_{c}$ and $v_{c}$ by one, and continue hashing at Step (3).
(5) Having found a matching seed at Step(4b), extend this match forwards and backwards from $\mathrm{v}_{\mathrm{m}}$ and $\mathrm{r}_{\mathrm{m}}$ as long as possible, reset $\mathrm{v}_{\mathrm{m}}$ and $\mathrm{r}_{\mathrm{m}}$ to the start offsets of the matching substring (if the match extended backwards), and set $l$ to the length of the matching substring.
(6) Encode the matching substring and attempt to use this substring to correct encodings in the encoding lookback buffer. One of the following three substeps is performed:
(a) If $\mathrm{v}_{\mathrm{s}} \leq \mathrm{v}_{\mathrm{m}}$, the matching substring overlaps only the previously unencoded suffix $V$; it cannot be used to correct encodings already in the buffer. If $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right.$ ) using an add command.

Encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ as a copy of the substring of length $l$ starting at offset $\mathrm{r}_{\mathrm{m}}$ in $R$. Output the command(s) to the buffer. Set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
(b) If $\mathrm{v}_{\mathrm{m}}<\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}+l$, the matching substring overlaps both the encoded prefix and the unencoded suffix of $V$. Perform tail correction. That is, attempt to correct encodings from the tail of the buffer by integrating commands into the new copy command. All whole and partial add commands and all whole copy commands that encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{s}}\right)$ can be integrated into the new copy command that also encodes the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}+l\right)$. Delete from the buffer all commands that were wholly integrated. Output the new copy command to the buffer. Set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
(c) If $\mathrm{v}_{\mathrm{m}}+l \leq \mathrm{v}_{\mathrm{s}}$, the matching substring overlaps only the existing encoded prefix of $V$. Perform general correction. That is, perform binary search in the buffer to find the commands that encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ and correct sub-optimal encodings when possible. (In this case, $\mathrm{v}_{\mathrm{s}}$ does not change.)
(7) Set $\mathrm{v}_{\mathrm{c}}$ to $\max \left(\mathrm{v}_{\mathrm{m}}+l, \mathrm{v}_{\mathrm{c}}+1\right)$ and $\mathrm{r}_{\mathrm{c}}$ to $\max \left(\mathrm{r}_{\mathrm{m}}+l, \mathrm{r}_{\mathrm{c}}+1\right)$; that is, we set the new values of these pointers to the offsets just following the matching substring, but we also require these pointers to advance by at least 1 . Return to Step (3).
(8) All of the input has been processed. Flush all commands from the buffer to the delta encoding. If $\mathrm{v}_{\mathrm{s}}<|\mathrm{V}|$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}},|\mathrm{V}|\right)$ with an add command. Terminate the algorithm.

Figure 2.3 Pseudocode for the correcting one-pass algorithm

### 2.3.4 - The Correcting 1.5-Pass Algorithm

The correcting 1.5 -pass algorithm can be seen as a reformulation of the greedy algorithm. The main difference is that it encodes the first matching substrings found, rather than searching exhaustively for the best matching substrings. While both algorithms make a pass over the reference string computing footprints and storing information in the hash table, the greedy algorithm stores, for each footprint, all offsets having that footprint; whereas the correcting 1.5-pass algorithm stores only the first such offset encountered. Hence it's linear running time.

The pseudocode of this algorithm follows.
Given a reference string $R$ and a version string $V$, generate a delta encoding of $V$ as follows:
(1) For each offset $a$, in input string $R$ in the interval $[0,|R|-p]$, generate the footprint $F_{R}(\mathrm{a}, \mathrm{a}+\mathrm{p})$. For each footprint generated, if the entry of $H_{R}$ indexed by that footprint is empty, store the offset in that entry:
for $\mathrm{a}=0,1, \ldots,|\mathrm{R}|-\mathrm{p}$ : if $H_{R}\left[F_{R}(\mathrm{a}, \mathrm{a}+\mathrm{p})\right]=$ empty then $H_{R}\left[F_{R}(\mathrm{a}, \mathrm{a}+\mathrm{p})\right]$ to a .
(2) Start $v_{c}$ and $v_{s}$ at offset zero.
(3) If $\mathrm{v}_{\mathrm{c}}+\mathrm{p}>|\mathrm{V}|$ go to Step (8). Otherwise, generate a footprint $\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$ at $\mathrm{v}_{\mathrm{c}}$.
(4) If $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty, check that the seed in $R$ at offset $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}\right.\right.$ $+\mathrm{p})$ ] is identical to the seed in $V$ at offset $\mathrm{v}_{\mathrm{c}}$. If matching seeds are found, continue at Step (5). Otherwise, increment $v_{c}$ by one and repeat Step (3).
(5) Extend the matching substring forwards and backwards as far as possible from the matching seed. Set $\mathrm{v}_{\mathrm{m}}$ and $\mathrm{r}_{\mathrm{m}}$ to the start of the matching substring in $V$ and
$R$, respectively, and set $l$ to the length of this substring. Note that $\mathrm{v}_{\mathrm{s}} \leq \mathrm{v}_{\mathrm{c}}<\mathrm{v}_{\mathrm{m}}+$ $l$ because $v_{c}$ never decreases, and because the match originated at the seed at offset $\mathrm{v}_{\mathrm{c}}$.
(6) Encode the match and attempt to correct bad encodings. The following two sub-steps are identical to sub-steps (6a) and (6b) in the correcting one-pass algorithm (sub-step (6c) cannot occur here, because $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}+l$ ):
(a) If $\mathrm{v}_{\mathrm{s}} \leq \mathrm{v}_{\mathrm{m}}$ : If $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right.$ ) using an add command. Encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ as a copy of the substring of length $l$ starting at offset $\mathrm{r}_{\mathrm{m}}$ in $R$. Output the command(s) to the buffer. Set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
(b) if $\mathrm{v}_{\mathrm{m}}<\mathrm{v}_{\mathrm{s}}$ : We have noted in Step (5) that $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}+l$. Attempt to correct encodings from the tail of the buffer. Delete from the buffer all commands that were wholly integrated. Output the new copy command to the buffer. Set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$.
(7) Set $\mathrm{v}_{\mathrm{c}}$ to $\mathrm{v}_{\mathrm{m}}+l$ and return to Step (3).
(8) All of the input has been processed. Flush all commands from the buffer to the delta encoding. If $\mathrm{v}_{\mathrm{s}}<|\mathrm{V}|$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}},|\mathrm{V}|\right)$ with an add command. Terminate the algorithm.

Figure 2.4 Pseudocode for the correcting 1.5-pass

### 2.4 Conclusion

This chapter reviewed recent differencing algorithms that operate at a fine granularity, make no assumptions about the format or alignment of input data and in
practice, run in linear time, use constant space, and give good compression. In the next chapter, we describe a test-bed of differential algorithms that combines ideas from the greedy differencing algorithm and the correcting one-pass differencing algorithm and provides an environment that allows us to obtain experimental results on the compression performance of the proposed algorithm versus the algorithms described in [1].

## CHAPTER III

## A Test-Bed

As has been seen in the previous chapters, several differencing algorithms have been written and implemented in order to achieve good compression results while seeking the best possible time and space complexities. This chapter introduces our contribution in this regards, which is a test-bed for a constant space, linear time differencing algorithms.

The test-bed is based on the idea that if the greedy algorithm yields optimal compression results while the one-pass algorithm maintains linear time and constant space, an interesting approach would be to find an algorithm that would give better compression results then the one-pass while maintaining linear time and constant space. So the test-bed is an environment that allows a tradeoff between the greedy and the one-pass algorithms. Also, the test-bed is important because it makes it possible to test new algorithms as well as the algorithms described in [1] and gives experimental results on their compression performance, hence the term test-bed. Future work on differencing algorithms can be experimented using this test-bed as well. This algorithm allows users to get very good compression results without having to sacrifice time and space complexities, which is quite a burden with large data inputs; as it maintains the bound on complexities without having to accept poor compression results.

## 3.1 - The Algorithm

The algorithm implementation relies on two major steps. In the first step, the algorithm builds two hash tables, called $\mathrm{H}_{\mathrm{R}}$ and $\mathrm{H}_{\mathrm{V}}$, for the reference file and the version file, respectively. The size of the hash tables is determined by the number of entries they have, which is the number of footprints generated from R and V , respectively. In the second step, the algorithm scans forward in both input strings R and V reading strings of constant length $p$, summarizes those seeds by footprinting them and then storing their offsets into $\mathrm{H}_{\mathrm{R}}$ and $\mathrm{H}_{\mathrm{V}}$, respectively, at their generated footprint. Each footprint (in $\mathrm{H}_{\mathrm{R}}$ or $\mathrm{H}_{\mathrm{V}}$ ) is an entry into the hash table and each footprint holds a linked list of constant size $L$ where the offsets are stored. The footprints in the hash tables are used to detect matching seeds, and when this happens, we try to extend the match as far as possible in both R and V . Two different seeds might yield the same footprint hence the need to store many offsets at one given entry. Unlike the algorithms described in [1], this algorithm maintains two linked lists, one for $\mathrm{H}_{\mathrm{R}}$ and one for $\mathrm{H}_{\mathrm{V}}$; having each a constant length $L$. All offsets scanned are stored and when the size of the linked list is exceeded, we overwrite the offset that has been used; this means that the string at that offset has been either copied or added therefore has been accounted for and its offset can be overwritten. This ensures that no offsets are overlooked. If no used offset is found on the linked list, the algorithm overwrites the oldest one inserted. Pseudocode for the test-bed algorithm follows.

Pseudocode for the test-bed algorithm

Given a reference string R and a version string V , generate a delta encoding of V as follows:
(1) Create empty hash tables, $\mathrm{H}_{\mathrm{R}}$ and $\mathrm{H}_{\mathrm{V}}$, for R and V , respectively. Initially, all entries are empty.
(2) Start pointers $r_{c}, v_{c}$, and $v_{s}$ at offset zero. Pointer $v_{s}$ marks the start of the suffix of $V$ that has not been encoded.
(3) If $\mathrm{v}_{\mathrm{c}}+\mathrm{p}>|\mathrm{V}|$ and $\mathrm{r}_{\mathrm{c}}+\mathrm{p}>|\mathrm{R}|$ go to Step (8). Otherwise, generate footprint $F_{V}$ $\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{v}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{V}|$ and footprint $F_{R}\left(\mathrm{r}_{\mathrm{c} .} \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ when $\mathrm{r}_{\mathrm{c}}+\mathrm{p} \leq|\mathrm{R}|$.
(4) At each footprint value maintain a linked list of constant size $L$ at $H_{R}$ and $H_{V}$ of all offsets that hashed to this value. When the size of the linked list is exceeded, overwrite the offsets flagged as used. If no flagged offset exists, overwrite the oldest one on the list.
(5) For footprints $F_{V}\left(\mathrm{v}_{\mathrm{c},}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)$ and $F_{R}\left(\mathrm{r}_{\mathrm{c},} \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)$ :
(a) If there is a hash table entry at the footprint value in the other string's hash table, the algorithm has found a likely matching substring. For example, $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty indicates a likely match between the seed at offset $\mathrm{r}_{\mathrm{c}}$ in $R$ and the seed at offset $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ in $V$. In this case set $\mathrm{r}_{\mathrm{m}}$ to $\mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{m}}$ to $H_{V}\left[F_{R}\left(\mathrm{r}_{\mathrm{c}}, \mathrm{r}_{\mathrm{c}}+\mathrm{p}\right)\right]$ to the start offsets of the potential match. Check whether the seeds at offsets $\mathrm{r}_{\mathrm{m}}$ and $\mathrm{v}_{\mathrm{m}}$ are identical because this hashing function is not ideal. If the seeds prove to be the same, matching substrings have been found. If this is the case, continue at Step (6) to extend the match (skipping the rest of Step (5)). Symmetrically, if $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right] \neq$ empty, set $\mathrm{v}_{\mathrm{m}}$ to $\mathrm{v}_{\mathrm{c}}$ and $\mathrm{r}_{\mathrm{m}}$ to $H_{R}\left[F_{V}\left(\mathrm{v}_{\mathrm{c}}, \mathrm{v}_{\mathrm{c}}+\mathrm{p}\right)\right]$. If the seeds at offsets $\mathrm{r}_{\mathrm{m}}$ and $\mathrm{v}_{\mathrm{m}}$ are
identical, continue at Step (6) to extend the match. At this point, no match starting at $v_{c}$ or starting at $r_{c}$ has been found. Increment both $r_{c}$ and $v_{c}$ by one, and continue hashing at Step (3).
(6) At this step, the algorithm has found a matching seed at offsets $v_{m}$ and $r_{m}$. The algorithm matches symbols forward in both strings, starting at the matching seed, to find the longest matching substring starting at $\mathrm{v}_{\mathrm{m}}$ and $\mathrm{r}_{\mathrm{m}}$. Let $l$ be the length of this substring.
(7) If $\mathrm{v}_{\mathrm{s}}<=\mathrm{v}_{\mathrm{m}}$, encode the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right.$ ) using an add command containing the substring $V\left[\mathrm{v}_{\mathrm{s}}, \mathrm{v}_{\mathrm{m}}\right)$ to be added. Encode the substring $V\left[\mathrm{v}_{\mathrm{m}}, \mathrm{v}_{\mathrm{m}}+l\right)$ as a copy of the substring of length $l$ starting at offset $\mathrm{r}_{\mathrm{m}}$ in $R$. Set $\mathrm{v}_{\mathrm{s}}$ to the offset following the end of the matching substring, that is, set $\mathrm{v}_{\mathrm{s}}$ to $\mathrm{v}_{\mathrm{m}}+l$. Set the flag of the offset of the substring encoded in both $H_{R}$ and $H_{V}$ to used and coded respectively. These are the nodes that will be overwritten when the linked list size is exceeded.
(8) Set $r_{c}$ and $v_{c}$ to the offset following the end of the match in $R$ and $V$ respectively $\left\{r_{c}\right.$ is allowed to move backwards in the file to the matching offset since a matching offset in $H_{R}$ may exist before the current pointer $r_{c}$. . That is set $\mathrm{r}_{\mathrm{c}}$ to $\mathrm{r}_{\mathrm{m}}+l$. and $\mathrm{v}_{\mathrm{c}}$ to $\mathrm{v}_{\mathrm{m}}+l$ \{provided $\mathrm{v}_{\mathrm{s}}<\mathrm{v}_{\mathrm{m}}$.\}
(a) If $v_{m}<v_{s}$, increment $v_{c}$ by one, and continue scanning $\left\{v_{c}\right.$ is not allowed to move back in the file. $\}$

Return to háshing again at Step (3).
(9) All input has been processed. Terminate the algorithm.

Figure 3.1 Pseudocode for the Test-Bed Algorithm

The implementation of this algorithm is done using $\mathrm{C}^{++}$and can be found in the Appendix.

## 3.2 - Time and Space Complexity

In this section we prove the following theorem.
THEOREM 5.1. The test-bed differencing algorithm runs in time $O(n)$ and Space $O(1)$, where $n$ is the total length of the input strings.

PROOF.
The space bound is clear. At all times, the algorithm maintains two hash tables, each of which has $q$ entries, having each a linked list of constant length $L$. This ensures a bound on the size of the hash tables. Except for the hash tables, the algorithm uses constant space. So, the total space used by the algorithm is $O(q * L)(=$ $O$ (1) if q and L are constants).

The time bound can be proved as follows. Initially, during Steps (1), the algorithm takes time O (q). In the subsequent steps, we follow the run of the algorithm and bound the time used in terms of the amount that the pointers $\mathrm{r}_{\mathrm{c}}$ and $\mathrm{v}_{\mathrm{c}}$ advance. When $r_{c}$ and $v_{c}$ are advancing in hashing mode, before a match is found, the algorithm uses time $O$ ( p ) each time that the pointers advance by one. When a matching seed is found, let $M=\max \left(v_{m}-v_{c}, r_{m}-r_{c}\right)$. Because either $v_{m}=v_{c}$ or $r_{m}=r_{c}$, then the total time spent in hashing mode is $\mathrm{O}(\mathrm{pM})$. The number of non-empty hash table entries at this point is at most $2 \mathrm{M}, \mathrm{M}$ in $\mathrm{H}_{V}$ and M in $\mathrm{H}_{\mathrm{R}}$. The match extension step takes time O ( $l$. The encoding step takes time $O\left(\mathrm{v}_{\mathrm{m}}-\mathrm{v}_{\mathrm{c}}\right)$; that is $\mathrm{O}(\mathrm{M})$. After a match, the pointers $\mathrm{v}_{\mathrm{c}}$ and $\mathrm{r}_{\mathrm{c}}$ are reset to the end of the match; let $\mathrm{v}_{\mathrm{c}}=\mathrm{v}_{\mathrm{m}}+l$ and $\mathrm{r}_{\mathrm{c}}=\mathrm{r}_{\mathrm{m}}+l$ be the values
of $v_{c}$ and $r_{c}$ after this is done at one given period. It follows that $v_{c}$ and $r_{c}$ are advanced by a total net amount of at least $M+2 l$ during the period. The time spent in the period is $\mathrm{O}(\mathrm{pM}+l)$. Let $\mathrm{M}^{*}$ be the sum of all $\mathrm{M}_{\mathrm{i}}$. Because the pointers can advance by a total net amount of at most $n=|R|+|V|$ during the entire run, then $\mathrm{M}^{*}+2 l \leq n$. It follows that the total time is $O(n p+q)=O(n)$.

## CHAPTER IV

## Experimental Results

The tests included in this chapter are conducted over text files of different sizes varying between 1 K and 100 K . For each file, we apply the following steps:

For a given set of files of size $s$, run the test-bed as follows:

1. Let the seed's length $p$ vary from 1 to 16 . For each value of $p$ go to Step (3)
2. Let the linked lists' sizes $L$ and $L^{\prime}$ of $\mathrm{H}_{\mathrm{R}}$ and $\mathrm{H}_{\mathrm{V}}$ respectively vary from 1 to $\infty$. Values are chosen randomly; in our tests we chose $L$ and $L$ ' to have this set of values $\{1,5,10,20,30,40, \infty\}$, where $\infty$ takes integer numbers big enough, such as 100,000 . For each value of $\{\mathrm{L}, \mathrm{L}$ ' $\}$ go to Step (3).
3. For a constant $L$ and $L$ ' and a fixed length $p$, generate the total number of copy commands \{number of copies \} and the total length of strings encoded with an add command \{total length added.\}
4. Compute the total cost of running the algorithm on the file. Total cost $=$ total copies + total length added.
5. The average cost per set of files of size $s$ is then computed.

## 4.1 - Tables and Graphs

The tests results are displayed in a table showing the average cost per set of files of size $s$. To compute the cost per file, a computation of the number of copy
commands, the number of add commands, and the total length of the strings added is done for each given value of p and for different values of $L$. The total cost is the summation of the total number of copies and the total length added. The average cost per file size is then computed.

### 4.1.1 - Files of Size 1K

- Average Cost Tables

| Table 4.1.1.1 - Average Values. $\mathrm{P}=1$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| L | 1 | 10 | $\infty$ |  |
| COPIES | 333 | 270 | 273 |  |
| ADDS | 63 | 87 | 86 |  |
| TOTAL <br> LENGTH <br> ADDED | 91 | 142 | 138 |  |
| TOTAL COST | 424 | 412 | 412 |  |


| Table 41.1.2 - Average Values. P $=2$ |  |  |  |
| :---: | :---: | :---: | :---: |
| L | 1 | 10 | 0 |
| COPIES | 73 | 67 | 63 |
| ADDS | 51 | 50 | 48 |
| TOTAL <br> LENGTH <br> ADDED | 247 | 266 | 249 |
| TOTALCOST | 320 | 332 | 312 |


| Table 4.1.1.3-Average Values. P $=3$ |  |  |  |
| :---: | :---: | :---: | :---: |
| L | 1 | 10 | 0 |
| COPIES | 34 | 33 | 33 |
| ADDS | 26 | 26 | 26 |
| TOTAL <br> LENGTH <br> ADDED | 309 | 311 | 311 |
| TOTAL COST | 343 | 344 | 344 |


| Table 4.1.1.4-Average Values. P $=8$ |  |  |  |
| :---: | :---: | :---: | :---: |
| L | 1 | 10 | $\infty$ |
| COPIES | 7 | 7 | 7 |
| ADDS | 6 | 6 | 6 |
| TOTAL <br> LENGTH <br> ADDED | 363 | 367 | 367 |
| TOTAL COST | 374 | 373 | 373 |


| Table 4.1.1.5-Average Values. $\mathrm{P}=16$ |  |  |  |
| :---: | :---: | :---: | :---: |
| L | 1 | 10 | 0 |
| COPIES | 4 | 4 | 4 |
| ADDS | 3 | 3 | 3 |
| TOTAL <br> LENGTH <br> ADDED | 264 | 260 | 260 |
| TOTAL COST | $\underline{267}$ | $\underline{264}$ | $\underline{264}$ |

## - Average Cost Graph

## Average Cost Graph



Figure 4.1 Average Cost Graph - Files of Size 1 K

### 4.1.2 - Files of Size 8 K

## - Average Cost Tables

| Table 4.1.2.1-Average Values. $P=1$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 4783 | 4002 | 3891 | 3810 | 3756 | 3608 | 3890 |
| ADDS | 900.3 | 1273 | 1189 | 1225 | 1164 | 1215 | 1225 |
| TOTAL <br> LENGTH <br> ADDED | 1853 | 2308 | 2202 | 2309 | 2276 | 2394 | 2206 |
| TOTAL COST | 6635 | $\underline{6310}$ | $\underline{6093}$ | $\underline{6120}$ | $\underline{6031}$ | 6003 | $\underline{6097}$ |


| Table 4.1.2.2-Aperage Values. $P=2$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 1310 | 1186 | 1156 | 1145 | 1181 | 1194 | 1201 |
| ADDS | 944 | 866 | 851 | 855 | 868 | 872 | 868 |
| TOTAL <br> LENGTH <br> ADDED | 4544 | 4254 | 4310 | 4336 | 4246 | 4217 | 4204 |
| TOTAL COST | 5854 | 5440 | 5465 | 5480 | 5427 | 5412 | 5405 |


| Table 41.2.3-Average Values. P $=3$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 434 | 416 | 426 | 420 | 423 | 425 | 426 |
| ADDS | 346 | 341 | 355 | 345 | 348 | 347 | 348 |
| TOTAL <br> LENGTH <br> ADDED | 5310 | 5338 | 5304 | 5323 | 5308 | 5298 | 5294 |
| TOTALCOST | 5744 | 5754 | 5730 | 543 | 5739 | 5723 | 5720 |


| Table 4.1.2. - Average Values. $\mathrm{P}=8$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 104 | 92 | 92 | 92 | 92 | 92 | 92 |
| ADDS | 93 | 86 | 86 | 87 | 87 | 87 | 87 |
| TOTAL <br> LENGTH <br> ADDED | 5947 | 6356 | 6392 | 6385 | 6385 | 6385 | 6385 |
| TOTAL COST | $\underline{6051}$ | $\underline{6448}$ | $\underline{6484}$ | $\underline{6477}$ | $\underline{6477}$ | $\underline{6477}$ | $\underline{6477}$ |


| Table 4.1.2.5-Average Values. $P=16$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 91 | 67 | 58 | 51 | 50 | 49 | 49 |
| ADDS | 44 | 48 | 46 | 46 | 46 | 45 | 45 |
| TOTAL <br> LENGTH <br> ADDED | 6164 | 6169 | 6232 | 6221 | 6211 | 6215 | 6215 |
| TOTALCOST | $\underline{6255}$ | $\underline{6236}$ | $\underline{6289}$ | $\underline{6272}$ | $\underline{6261}$ | $\underline{6264}$ | $\underline{6263}$ |

## - Average Cost Graph



Figure 4.2 Average Cost Graph - Files of Size 8K

### 4.1.3 - Files of Size 30K

- Average Cost Tables

| Table 4.1.3.1 - Average Values. $\mathrm{P}=1$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\stackrel{+}{4}$ | , | 4 |  |  |  |  |
| $\mathrm{L}$ | +1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 20416 | 18066 | 16333 | 15365 | 15076 | 15470 | 15646 |
| $\square \mathrm{ADDS}$ | 2873 | 2870 | 2999 | 3282 | 3129 | 3203 | 3146 |
| TOTAL LENGTH. ADDED. | 4624 | 4566 | 4734 | 5167 | 4999 | 5087 | $4911$ |
| TOTAL COST | 25039 | 22632 | 21067 | 20532 | 20075 | 20557 | 20558 |


| Table 411.3.2 Average Values, $P=2$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - |  |  |  |  |  |  |  |
| $\because, \square$, | Y 1 | 5 5 | 10 | 20. | 30 | $40$ | ¢ ${ }^{\circ}$ |
| COPIES | 7336 | 6704 | 6521 | 6377 | 6277 | 6373 | 6717 |
| ADDS | $3471$ | 3483 | $35 \geq 6$ | 3578 | 3591 | 3602 | 3477 |
| TOTAL LENGTH ADDED | 10703 | 11200 | 11514 | 11852 | 12062 | 11840 | 11079 |
| TOTAL COST | 18039 | 17004 | 18035 | 18229 | 18339 | 18213 | 17797 |


| 4, $4 \cdot 3$ - Averas |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 2806 | 2672 | 2641 | 2563 | 2514 | 2574 | 2702 |
| ADDS | 2140 | 2076 | 2069 | 2033 | 2015 | 2039 | 2082 |
| $\begin{aligned} & \text { TOTAL } \\ & \text { LENGTH } \\ & \text { ADDED } \end{aligned}$ | 17502 | 17778 | 17838 | 18092 | 18291 | 18077 | 17608 |
| TOTAL COST | 20308 | 20450 | 20479 | 20655 | 20805 | 20651 | $\underline{20310}$ |


| Table 4.1.3.4-Average Values. $\mathrm{P}=8$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $L$ | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 257 | 264 | 257 | 264 | 254 | 257 | 256 |
| ADDS | 247 | 254 | 244 | 257 | 247 | 249 | 248 |
| TOTAL <br> LENGTH <br> ADDED | 26744 | 26631 | 26681 | 26712 | 26665 | 26755 | 26656 |
| TOTAL COST | $\underline{27001}$ | 26895 | 26932 | 26977 | 26919 | 27012 | 26911 |


|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 39 | 34 | 35 | 35 | 35 | 35 | 35 |
| ADDS | 30 | 31 | 32 | 33 | 33 | 33 | 33 |
| TOTAL LENGTH ADDED | 25480 | 26003 | 25975 | 25969 | 25968 | 25968 | 25968 |
| TOTAL COST | 25519 | 26038 | 26010 | $\underline{26004}$ | $\underline{26004}$ | 26004 | 26004 |

## - Average Cost Graph



Figure 4.3 Average Cost Graph - Files of Size 30K

### 4.1.4 - Files of Size 40K

- Average Cost Tables

| Table 4.1.4:2 A Aerage Values, $P=1$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| . | +\%. |  |  | T\% | , | m. | +3. |
| ¢ |  | + | - | ¢ |  | Tre | T |
| $\therefore<1$ | 1 | 5 | 10. | 20 | 30 | 40 | $\pm$ |
|  |  |  |  |  |  |  |  |
| COPIES | 15932 | 22214 | 20663 | 19514 | 19077 | 18891 | 19487 |
| namum |  |  | + |  | W |  |  |
| A ADDS | 2786 | 4784 | $47^{80}$ | 4896 | 4801 | 4797 | 5018 |
| I TOTAL | \% |  | + | Tmiz |  |  |  |
| Length | 17216 | 8309 | 8294 | 8518 | 8472 | 8544 | 8688 |
| ADDEED | Y, | - |  |  | - |  | + |
|  |  |  | 0 | + | W |  |  |
| TOTALCOST | 33147 | 30522 | 28958 | 28032 | 38549 | 27435 | 28175 |


|  | Table |  |  |  |  |  | $4$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4 |  |  |  |  |  |  |
| $L$ | 11 1 |  | $10$ |  |  | $x^{4}$ |  |
|  |  |  |  |  |  |  |  |
| COPIES | 9691 | 8902 | 8672 | 8391 | 83 2 | 8216 | 879 |
|  |  |  |  |  |  |  |  |
| ADD | 446 | 4393 | 4431 | 4449 | 4500 | 4554 | 4376 |
| TOTAL |  |  |  |  |  |  |  |
| LENGTH | 14122 | 14940 | 15137 | 15491 | 15959 | $16 \geq 38$ | 14824 |
| ADDED | - |  | + |  | + |  |  |
|  |  |  |  |  |  |  |  |
| TOTALCOST | 23813 | 23842 | 23809 | 23882 | 24282 | 24454 | 3362 |


| Table 4.1.4.3-Average Values. $P=3$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | $30$ | 40 | 0 |
| COPIES | 4154 | 4112 | 3963 | 3881 | 3828 | 3850 | 4030 |
| ADDS | 3009 | 2923 | 2891 | 2885 | 2862 | 2886 | 2903 |
| $\begin{aligned} & \text { TOTAL } \\ & \text { LENGTH } \\ & \text { ADDED } \end{aligned}$ | 21512 | 21074 | 21500 | 21785 | 21955 | 21871 | 21240 |
| TOTAL COST | 25665 | $\underline{25186}$ | 25462 | 25666 | 25783 | 25722 | 25270 |


| Table 4.1.4-4-Arerage Values. $\mathrm{P}=\mathrm{B}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | - |  | \% |  |  |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 292 | 339 | 336 | 339 | 331 | 331 | 343 |
| ADDS | 277 | 326 | 195 | 328 | 321 | 319 | 330 |
| $\begin{aligned} & \text { TOTAL } \\ & \text { LENGTH } \\ & \text { ADDED } \\ & \hline \end{aligned}$ | 35242 | 34954 | 34894 | 34950 | 34976 | 34978 | 34933 |
| TOTAL COST | 35.535 | 35292 | 35231 | 35289 | 35308 | 35309 | 35276 |


| Table 4.1.4.5-Average Values. $P=16$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 9 | 21 | 18 | 18 | 16 | 18 | 16 |
| ADDS | 8 | 17 | 17 | 17 | 15 | 17 | 15 |
| TOTAL <br> LENGTH <br> ADDED | 27137 | 35047 | 31530 | 31523 | 30709 | 31210 | 30709 |
| TOTAL COST | 37145 | 35068 | 31548 | 31542 | 30725 | 31228 | 30725 |

## - Average Cost Graph



Figure 4.4 Average Cost Graph - Files of Size 40K

### 4.1.5 - Files of Size 70K

## - Average Cost Tables

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1, | $=$ | 10 | 20 | 30 | $40$ | $\infty$ |
| COPIES | 50198 | 43403 | 40460 | 39027 | 38439 | 37990 | 38322 |
| DDS |  |  |  | \% |  |  |  |
| ADDS | 7270 | 3 O 44 | 7934 | 7813 | 7907 | 7944 | 7994 |
| TOTAL |  |  |  |  |  |  |  |
| LENGTH | 10343 | 11800 | 11760 | 11561 | 11757 | 11849 | 12199 |
| ADDED |  |  |  | 㕸 | , | . | - |
|  |  |  |  |  |  |  |  |
| TOTAL COST | 60.544 | 55203 | 52220 | 50588 | 50196 | 49839 | 50520 |


|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| W ${ }^{4}$ | 4 417 |  | m. | \% |  | 4] |  |
| \%. | \% |  |  |  |  |  |  |
| L\#\# | 1 | \% 5 | 10 | 20 | 30. | $4{ }^{4}$ | $\cdots$ |
|  |  |  |  |  |  |  |  |
| COPIES | 18695 | 16039 | 14556 | 16232 | 14922 | 14708 | 14508 |
|  |  |  |  |  |  |  |  |
| ADDS | 8274 | 8111 | 8031 | 8479 | 3565 | 8535 | 7948 |
| THOTAL |  |  |  |  |  |  | +1314 |
| LENGTH | 23804 | 27703 | 30911 | 26539 | 29680 | 30112 | 30949 |
| Q ADDED |  | +x | $\because$ | 1 |  |  |  |
|  |  |  |  |  | 1 |  |  |
| TOTAL COST | 42499 | 43742 | 45467 | 42770 | 44602 | 44820 | 45457 |


|  | Table 4.1.5.3-Average Values. $P=3$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |  |
| COPIES | 7561 | 7130 | 6919 | 6690 | 6579 | 6551 | 6955 |  |
| ADDS | 5630 | 5436 | 5356 | 5241 | 5216 | 5224 | 5352 |  |
| TOTAL <br> LENGFH <br> ADDED | 40068 | 40989 | 41414 | 42216 | 42620 | 42797 | 41261 |  |
| TOTAL COST | 47629 | 48119 | 48333 | 48906 | 49198 | 49348 | 48216 |  |


| Table 4.1.5-4-Average Values. $P=8$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | \% |  | $\cdots$ |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\omega$ |
| COPIES | 740 | 637 | 662 | 603 | 589 | 614 | 603 |
| ADDS | 642 | 606 | 631 | 584 | 573 | 598 | 588 |
| TOTAL LENGTH ADDED | 63763 | 64176 | 63635 | 64264 | 64413 | 64225 | 64322 |
| TOTAL COST | 64503 | 64813 | 64297 | 64867 | 65002 | 64839 | 64925 |


| - Table 4.1.5.5-Average Values. $P=16$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 61 | 61 | 74 | 65 | 56 | 58 | 52 |
| ADDS | 53 | 48 | 50 | 50 | 46 | 48 | 43 |
| TOTAL LENGTH ADDED | 48693 | 52126 | 55478 | 58035 | 61002 | 57291 | 47301 |
| TOTAL COST | 48754 | 52187 | 55552 | 58100 | 61058 | 57349 | 47353 |

## - Average Cost Graph



Figure 4.5 Average Cost Graph - Files of Size 70K

### 4.1.6 Files of Size 100 K

- Average Cost Tables

| Table 4.1.6.1-Average Values. $\mathrm{P}=1$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 75907 | 66759 | 62858 | 57717 | 57322 | 56718 | 57946 |
| ADDS | 10841 | 10986 | 10454 | 11933 | 10982 | 12124 | 12336 |
| TOTAL <br> LENGTH <br> ADDED | 16579 | 17989 | 16945 | 19606 | 17898 | 20443 | 20692 |
| TOTAL COST | $\underline{92486}$ | $\underline{84748}$ | 79803 | 77323 | $\underline{75220}$ | $\underline{77161}$ | 78639 |


| Table 4.1.6.2-Average Values. $\mathrm{P}=2$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 29440 | 27245 | 26553 | 26197 | 25797 | 25714 | 26555 |
| ADDS | 11769 | 12239 | 12473 | 12243 | 12400 | 12412 | 12334 |
| TOTAL <br> LENGTH <br> ADDED | 35319 | 37491 | 38702 | 38379 | 39487 | 39326 | 38024 |
| TOTAL COST | $\underline{64760}$ | $\underline{64736}$ | $\underline{65255}$ | $\underline{64576}$ | $\underline{65284}$ | $\underline{65039}$ | $\underline{64578}$ |


| Table 4.1.6.3-Average Values. P=3 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | 0 |
| COPIES | 12227 | 11767 | 11449 | 11306 | 11205 | 11267 | 11601 |
| ADDS | 8552 | 8341 | 8236 | 8205 | 8250 | 8293 | 8296 |
| TOTAL <br> LENGTH <br> ADDED | 58004 | 60669 | 61564 | 62024 | 62404 | 62069 | 61016 |
| TOTAL COST | 70232 | 72436 | 73013 | 73331 | 73608 | 73336 | 72618 |


| Table 4.1.6-Average Values. $\mathrm{P}=8$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 919 | 1423 | 1363 | 1353 | 1385 | 1326 | 4558 |
| ADDS | 830 | 1349 | 1300 | 1294 | 1321 | 1263 | 3555 |
| TOTAL <br> LENGTH <br> IDDED | 95638 | 97533 | 98596 | 98638 | 98456 | 98735 | 87155 |
| TOTAL COST | 96556 | 98956 | 99958 | 99991 | 99841 | 100061 | 91713 |


| Table 4.1.6.5-Average Values. $P=16$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L | 1 | 5 | 10 | 20 | 30 | 40 | $\infty$ |
| COPIES | 43 | 109 | 69 | 87 | 93 | 76 | 77 |
| ADDS | 41 | 75 | 67 | 83 | 89 | 72 | 73 |
| TOTAL <br> LENGTH <br> ADDED | 95977 | 96347 | 91292 | 95227 | 95186 | 88528 | 88524 |
| TOTALCOST | 96090 | 96456 | 91362 | 95314 | 95278 | $\underline{88604}$ | $\underline{88600}$ |

- Average Cost Graph


Figure 4.6 Average Cost Graph - Files of Size 100K

### 4.2 Recommendations

Based on the above set of experiments, some recommendations can be made as to the values of $p$ and $L$ that relatively yield good compression results. Next, and for each set of files of size $s$, we highlight which values of $p$ and $L$ give good compression results while maintaining linear time and constant space.

### 4.2.1 - Files of Size 1K

The experimental results show that a good average compression cost of files of size 1 K , is achieved for a seed's length $p=2$ and for a constant linked list size $\mathrm{L}=40$. The values are as follows:

Good Average Cost: 264 for $p=16$ and $L=10$

### 4.4.2 - Files of Size 8 K

A good average compression cost is achieved for the following values:
Good Average Cost: 5412 for $p=2$ and $L=40$

### 4.2.3 - Files of Size 30K

A good average compression cost is achieved for the following values: Good Average Cost: 17904 for $p=2$ and $L=5$

### 4.4.4 - Files of Size 40K

A good average compression cost is achieved for the following values: Good Average Cost: 23809 for $P=2$ and $L=10$

### 4.4.5 - Files of Size 70K

A good average compression cost is achieved for the following values:
Good Average Cost: 42499 for $P=2$ and $L=1$

### 4.4.6 - Files of Size 100K

A good average compression cost is achieved for the following values:
Good Average Cost: 64576 for $p=2$ and $L=20$

## CHAPTER VI

## Conclusion

In this thesis, we have created a test-bed for differencing algorithms that run in linear time and use constant space. We have discussed the delta encoding differencing technique. Our experimental results provided the best values for the length of the linked list and the length of the seed to be used in the hash tables as function of the input size.

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## APPENDIX

## A TEST-BED FOR LINEAR TIME CONSTANT SPACE DIFFERENCING ALGORITHMS

\#include "list.cpp"<br>\#include "Node.h"<br>\#include "Vlist.cpp"<br>\#include "VNode.h"<br>\#include "declarations.h"<br>\#include <iostream.h><br>\#include <fstream.h><br>\#include <iomanip.h><br>\#include <stdlib.h><br>\#include <string.h><br>\#include <math.h><br>\#include <stdio.h><br>\#include <limits.h>

/*
Main()
*/
main()
\{
ifstream readReference("reference.txt", ios::in), readVersion("version.txt", ios::in);

```
if(!readReference)
{
```

cerr<<"File could not be opened"<<endl;
exit(1);
\}//endif
if(!readVersion)
\{
cerr<<"File could not be opened"<<endl; exit(1);
\}//endif
readReference.read((char*)\&current, p);
readVersion.read((char*) \& versionstring, p$)$;
//BUILD THE HASH TABLES INCREMENTALLY
proceed(readReference, readVersion, HR,HV,current, versionstring, rc, vc, p);
cout<<" $\ln \backslash n \backslash a l t$ n----------....... Total \# of Copies for this File are:
'"<<COPYCOUNTER<<"'"<<endl;
cout<<" $\ln \ln \backslash n \backslash t n---------------$ Total \# of Adds for this file are:
'"<<ADDCOUNTER<<"'"<<endl;
cout<<" $\ln \backslash n \backslash n \mid t n----------------$ Total Length of the Strings Added for this file are: '" $\ll$ TOTALLEN $\ll$ "'" $\ll e n d l$;

return 0 ;
\}//endofmain()
/*
End of Main()
*/
/*
Proceed()
*/
void proceed(ifstream readReference, ifstream readVersion, List HR[LISTSIZE], VList HV[LISTSIZE], Seed current, VerSeed versionstring, int rc, int vc, int p)

```
while ((!readReference.eof())
    && (!readVersion.eof()))
{
    //cout<<"\nln --------------------------------------------------------------------------
//getchar();
// cout<<"\n Current REFERENCE String is: ";
outputline(cout, current);
//rc is the starting offset of each scanned string in the file
rc = readReference.tellg() - p;
cout<<" At Offset RC = "<<rc;
cout<<" ";
//Compute footprint of the reference seed
unsigned long fprintR = footprint(current,rc, p);
cout<<" With Footprint = "<<fprintR;
HR[fprintR].insertAtFront(rc); //insert rc into hash table H}\mp@subsup{H}{R}{
                                    //at its footprint fprintR
cout<<"\n\n Current VERSION String is: ";
outputline2(cout, versionstring);
vc = readVersion.tellg() - p;//Vc is the starting offset of a scanned
                                    //string in the file
cout<<" At Offset VC = "<<vc;
//compute a Version seed's footprint
unsigned long fprint V = footprint2(versionstring,vc, p);
cout<<" With Footprint = "<< fprintV<<endl;
HV[fprintV].VinsertAtFront(vc);
```

//Check for each seed scanned in the version file whether its footprint //exists in the hash table of R.
//And simultaneously, for each seed scanned in the reference file, $/ /$ check whether its footprint exists in the hash table of $V$.
//This ensures we are maintaining a window into the past for finding //transposed seeds

```
// 1) Search for fooptrint fprintV in hash table HR[]
```

```
//if firstptr != 0 then fprintV exists in HR
if (!HR[fprintV].isEmpty())
{
cout<<" \n\n Footprint from HV[] "'<<fprintV<<"' was found in
HR[]. In\nlt Examine offsets in HR[]: \n"<<endl;
\[
\begin{array}{r}
\text { Rptr }=\mathrm{HR}[\text { fprintV].Fptr(); } / / \mathrm{Rptr}=\text { first node on the list } \\
\text { ///of HR[fprintV] }
\end{array}
\]
int offR = HR[fprintV].getOffset(Rptr);//offR = offset
                                    //stored at Rptr
```

//now go in V to the offset stored at HV[fprintV]
Vptr $=\mathrm{HV}[f \mathrm{fprintV}] . \mathrm{VFptr}() ; \quad / / \mathrm{VNode}=$ first node on the
//hist of HV[fprintV]
int offV $=\mathrm{HV}[f p r i n t V] . V g e t O f f s e t(V p t r) ; \quad / / / o f f V=$ offset
// stored at Vptr

## while (Rptr != 0) //while an offset exists on the next node of //the list at $\mathrm{HR}[f \mathrm{fprintV}$ ]

//search the list for a node that has not yet been encoded //i.e. used=false.
//if no such node is found encode the used ones on the //list.

```
offR = HR[fprintV].getOffset(Rptr); //get next offset
                                    //in the list
rm = offR; //a possible match exists: set rm = offR
vm = offV; //a possible match exists; set vm = offV;
if (vs <= vm)
{
    readReference.seekg(offR); //go to offR in R
    readVersion.seekg(offV); //go to offV in V
```

```
                    //scan from both files a string of length p=3
                    readReference.read((char*)&indexedseed, p);
readVersion.read((char*)&indexedverseed,p);
Encode(Rptr,Vptr,readReference, readVersion, HR, HV, indexedseed, indexedverseed,rc,vc, rm, vm, p, fprintR, fprintV);
//keeping record of the longest match only. if ((len >= leng) \&\& (len !=0))
\(\{\)
for (int \(\mathrm{cp}=0 ; \mathrm{cp}<\) len; \(\mathrm{cp}++\) ) tempstring \([\mathrm{cp}]=\) REFlongestmatch \([\mathrm{cp}]\);
tempstring[len] = ' 10 ';
matchingR \(=\mathrm{rm}\);
matching \(V=\mathrm{vm}\);
longestRptr \(=\) Rptr;
longestVptr \(=\) Vptr;
leng \(=\) strlen(tempstring);
\}//endif()
else; \(\quad / /\) if length of a new string is smaller //than its predecessor disregard it
\}//endif(vs<vm)
else; \(\quad / / i f\) vm<vs don't accept it. We only //move forward in V
\(\mathrm{Rptr}=\mathrm{HR}[\mathrm{fprint} \mathrm{V}] . \mathrm{nPtr}(\mathrm{Rptr}) ; \quad / /\) next pointer
offR = HR[fprintV].getOffset(Rptr); //next offset \}//endwhile()
if \(((\) leng \(>0) \& \&(\mathrm{vm}>=\mathrm{vs}))\)
\{
//Before Copy-encoding a matching seed, Add() the //string [Vs,Vm)
int \(\mathrm{l}=\mathrm{vm}-\mathrm{vs} ; / / \mathrm{l}=\) length of \(\operatorname{string}[\mathrm{Vs}, \mathrm{Vm}-1]\)
if \((\mathrm{l}==0)\) cout<<" \(\ln \ln \backslash t\) No String TO ADD.";
```

```
            else
            {
            int curr = readVersion.tellg();
            int Rcurr = readReference.tellg();
                    readVersion.seekg(vs); //position pointer at Vs
                    int initial = readVersion.tellg(); //vs value
                    readVersion.read((char*)&vstring,l); //scan
                        //seed [Vs,Vm)
                    ADD(vstring,l,vs);
                    int stln = strlen (vstring.VerSubstring);
                    for (int i=0;i<=stln; i++)
                        vstring.VerSubstring[i] = '10';
                    readVersion.seekg(curr); //reposition the pointer
    }//endof Else()
            COPY(tempstring, leng,matchingR); //matchingR =
                                    //offset of the longest
                                    //string stored in REFlong
            //Set Flags in HR & HV
            HR[fprintR].setflag(longestRptr,matchingR);
            HV[fprintV].Vsetflag(longestVptr,matchingV);
            vs = matchingV + leng;// + 1;
            vc=vs + p-1;
            rc = matchingR + leng + p-1; //rc moves backwards
            readVersion.seekg(vc);
            readReference.seekg(rc);
    }//endif(leng>0)
    else;
}//endif(!HR[fprintV].isEmpty())
else
{
    cout<<"\n\n FOOTPRINT from HV[] NOT FOUND IN
    HR[]"<<endl;
}
```

```
for (int \(\mathrm{e}=0 ; \mathrm{e}<=\) SIZE; \(\mathrm{e}++\) ) //re-initialize tempstring[]
    tempstring[e] = ' 10 ';
leng \(=0 ; \quad / /\) re-initialize leng
for (int ee \(=0\); ee \(<=\) SIZE; ee++) //re-initialize REFlongestmatch
    REFlongestmatch[ee] = '10';
len \(=0\);
```

//2) Search for fooptrint fprintiR in hash table HV[]

```
//if firstptr != 0 then fprintR exists in H}\mp@subsup{H}{V}{
```

if (!HV[fprintR].VisEmpty())
\{
cout<<" $\ln \ln$ Footprint from HR[] '"<<fprintR<<"' was found in
HV[]. In\nlt Examine offsets in HV[]: $\ln " \ll e n d l$;
//get first offset from $H_{V}$ at fprintR in the first node of the list;
VVptr = HV[fprintR].VFptr();
int of $V=H V[$ fprint $R] . V$ getOffset(VVptr);
RRptr $=\mathrm{HR}[$ fprintR].Fptr();
int ofR $=H R[$ fprint $R]$.getOffset $(R R p t r)$;
while (VVptr !=0)
\{
//search the list for a node that has not yet been encoded
//i.e. used=false.
//if no such node is found we encode the used ones on the
//list.
$\mathrm{vm}=\mathrm{ofV} ; \quad / / \mathrm{a}$ possible match exists
$\mathrm{rm}=\mathrm{ofR}$;
$/ / \mathrm{Go}$ in R to the offset stored at $\mathrm{H}_{\mathrm{R}}$ [fprintR]
if ( $\mathrm{vs}<=\mathrm{vm}$ )
\{
readVersion.seekg(ofV);
readReference.seekg(ofR);
// scan from R \&V a string of length $\mathrm{p}=3$
readReference.read((char*)\&Rseed, $p$ );
readVersion.read((char*)\&Vseed,p);

```
                    Encode(RRptr,VVptr,readReference, readVersion,
                    HR, HV, Rseed, Vseed,rc,vc, rm, vm, p, fprintR,
                    fprintV);
            if (len >= ln)
            {
                for (int ss = 0; ss < len; ss++)
                                    returned[ss] = REFlongestmatch[ss];
                                    returned[len] = '\0';
                matchingR = rm;
                matchingV = vm;
                longestRptr = RRptr;
                longestVptr = VVptr;
                ln = strlen(returned);//update length of returned[]
    }
    else;
    }//endif(vs<=vm)
    else;
    //VVptr =next node-offset in the list at fprintR
    VVptr = HV[fprintR].VnPtr(VVptr);
    ofV = HV[fprintR].VgetOffset(VVptr);
}//endwhile()
if ((leng > 0) && (vm >= vs))
{
    //Before Copy-encoding a matching seed, Add() the
    //string [Vs,Vm)
    int l = vm-vs; }\quad//l=\mathrm{ length of string [Vs Vm-1]
    if (l== 0)
    cout<<"\n\n\t No String TO ADD.";
    else
    {
    int curr = readVersion.tellg();
    int Rcurr = readReference.tellg();
    readVersion.seekg(vs); //position the file pointer at VS
    int initial = readVersion.tellg();
    readVersion.read((char*)&vstring,l); //get string [Vs,Vm)
```

ADD(vstring,l,vs); int stlng = strlen(vstring. VerSubstring);
for (int $\mathrm{i}=0 ; \mathrm{i}<=$ stlng; $\mathrm{i}++$ )
vstring. VerSubstring[i] = ' 10 ';
readVersion.seekg(curr); //reposition the pointer
\}//endof Else()

COPY(returned, ln,matchingR);
//Set flags in both $H_{R} \& H_{V}$
HR[fprintR].setflag(longestRptr,matchingR);
HV[fprintV].Vsetflag(longestVptr,matchingV);
$\mathrm{vs}=$ matching $\mathrm{V}+\ln ; / / \mathrm{ln}=$ length of the matching seed $\mathrm{vc}=\mathrm{vs}+\mathrm{p}-1$;
$\mathrm{rc}=$ matching $\mathrm{R}+\ln +\mathrm{p}-1 ; \quad / / \mathrm{rc}$ moves backwards
readVersion.seekg(vc); //re-position pointer inV readReference.seekg(rc); //re-position pointer in R

```
        }//endif(leng>0)
else
}//endif(!HV[fprintR].isEmpty())
else
{
        cout<<"\n\n FOOTPRINT from HR[] NOT FOUND IN HV[]"<<endl;
}
for (int f=0; f <= SIZE; f++) //re-initialize
    returned[f] = '10';
ln=0;
//re-initialize
for (ee = 0; ee <= SIZE; ee++) //re-initialize
REFlongestmatch[ee] = '10';
len = 0;
int vv = readVersion.tellg() - p + 1;
```

```
            readVersion.seekg(vv);
            int rr = readReference.tellg() - p + 1;
            readReference.seekg(rr);
            readReference.read((char*)&current, p);
            readVersion.read((char*)&versionstring, p);
            }//endofwhile()-------->> end of file is reached.
}//endof Proceed()
```

```
/*
    Encode()
*/
```

void Encode(Node * rrptr, VNode * Vyptr,ifstream readReference, ifstream readVersion, List HR[LISTSIZE], VList HV[LISTSIZE], Seed current, VerSeed versionstring, int rc, int vc, int rcm, int vcm, int $p$, int fprintR, int fprintV)
\{

```
ExtendMatch stretch;
ExtendMatch2 grow;
//Check if two strings match
cmp = CompareSeeds(current, versionstring);
if(vcm >= vs)
{
    if (cmp == 0) //The two strings match
    {
            rcmatch = rcm;
            vcmatch = vcm;
            cout<<"\n\n\t MATCHING SEEDS FOUND !!!";
```

```
for (int m=0; m < 3;m++)
{
    matchREF[m] = current.substring[m];
    matchVER[m] = versionstring.VerSubstring[m];
}//endfor
```

strcpy(REFlongestmatch,matchREF);
strcpy(VERlongestmatch,matchVER);
int off;
int Voff;
off $=$ readReference.tellg ()$-\mathrm{p}$; //offset of the matching seed in R
Voff $=$ readVersion.tellg() - p; //offset of the matching seed in $V$
int Vextensionpoint $=v \mathrm{~cm}+\mathrm{p}$;
int Rextensionpoint $=\mathrm{rcm}+\mathrm{p}$;
readReference.seekg(Rextensionpoint);
readVersion.seekg(Vextensionpoint);
while (1)
\{
readReference.read((char*) $\&$ stretch, 1); //check next
//character
readVersion.read((char*) $) \&$ grow, 1$) ; / /$ check next
//character
//if next characters don't match, extension not possible. if (stretch.Rlongest[0] != grow.Vlongest[0]) \{ break;
\}
else
\{
strncat(REFlongestmatch,stretch.Rlongest,1);
strncat(VERlongestmatch, grow.Vlongest,1);
if((readReference.eof()) \|(readVersion.eof()))
\{
break;

$$
\begin{array}{l}\text { \}//endif() } \\ \text { \}//endelse() } \\ \text { \}//endWhile() } \\ \text { //len = length of the longest matching string } \\ \text { len = strlen(REFlongestmatch); }\end{array}
$$

```
        }//endif(cmp==0)
        else //strings don't match
        {
        cout<<"\n\n\n\n\t STRINGS DON'T MATCH !!! ";
        rc = rc + p; //advance rc by p since we scan strings from
        //current location - length + 1
            readReference.seekg(rc);
```

                \(\mathrm{vc}=\mathrm{vc}+\mathrm{p} ; / /\) advance vc by p
                readVersion.seekg(vc);
    \}//endElse()
    \}//endif(vem>=vs)
            else ; \(\quad / / \mathrm{vm}<\mathrm{vs}\), disregard.
    \}//endof Encode()
/*
footprint()
*/
unsigned long footprint(Seed curr, int $\mathbf{r}$, int p )
\{
$\mathrm{F}=0$; //the footprint of a scanned seed
int $\mathrm{q}=1001$; // number of entries in the hash table
$/ / r=$ current offset $\&$ corresponds to $j=0$ of the seed stored in substring[j] of
//length $\mathrm{p}=3$
//and $\mathrm{i}<=\mathrm{r}+\mathrm{p}-1$ corresponds $\mathrm{j}<=\mathrm{p}-1$.
int $\mathrm{j}=0$;

```
    while (j <= p-1)
        if(j<=p-1)
        {
            int i = r;
                while (i<=r + p-1)
                {
                F += pow(127,r + p - 1-i)* curr.substring[j];
                i++;
                j++;
            }//endwhile()
            j++;//j>2: Get next string
    }//endFor()
        return F % q;
}//end of footprint()
```

/*
Footprint2()
*/
unsigned long footprint2(VerSeed $S$, int $r$, int $p$ )
\{
$\mathrm{Fv}=0$; //the footprint of a scanned seed
int $\mathrm{q}=1001$; // number of entries in the hash table
$/ / r=$ current offset \& corresponds to $\mathrm{j}=0$ of the seed stored in substring[j] of
//length $\mathrm{p}=3$
//and $\mathrm{i}<=\mathrm{r}+\mathrm{p}-1$ corresponds $\mathrm{j}<=\mathrm{p}-1$.
int $\mathrm{j}=0$;
while ( $\mathrm{j}<=\mathrm{p}-1$ )
if $(j<=p-1)$
\{
int $\mathrm{i}=\mathrm{r}$;

```
            while (i<= r + p-1)
            {
                        Fv += pow (127,r + p-1-i)*S.VerSubstring[i];
                i++;
                - j++;
                    }//endwhile()
                    j++;//j>2 : get the next string
    }//endFor()
    return Fv % q;
}//end of footprint2()
/*
                                    Outputline()
    */
    void outputline(ostream &out, Seed s)
    {
        out<<"'"<<s.substring<<"'";
    }//endof outputline()
    /*
        Outputline2()
    */
    void outputline2(ostream & print, VerSeed vs)
    {
```

print<<"" $\ll$ vs.VerSubstring<<""";
\}//endof outputline2()

```
/*
    CompareSeeds()
*/
int CompareSeeds(Seed cs, VerSeed Vcs)
{
    int comp;
    comp = strcmp(cs.substring, Vcs.VerSubstring);
    return comp;
}//endofCompareSeeds()
/*
Copy()
*/
```

void COPY (char * REFstr, int leng, int addr)
\{
COPYCOUNTER++;
cout<<"\n\n\n------COPY MATCHING REFERENCE STRING------";
cout<<" $\ln \ln$ COPY '" $\ll$ REFstr<<""";
cout<<"ln (C,"<<leng<<","<<addr<<")"<<endl;
cout<<"ln TOTAL LENGTH ENCODED WITH A COPY() is: "<<leng<<endl;
cout<<"ln TOTAL NUMBER OF COPIES = "<<COPYCOUNTER<<endl;
\}//end of Copy()
void ADD(VerSeed Vstr,int LEN,int q)
\{
ADDCOUNTER++; TOTALLEN += LEN;

cout<<" $\ln \ln (\mathrm{A}, " \ll \mathrm{LEN} \ll ", " \ll$ Vstr.VerSubstring<<<")"<<endl;
cout $\ll$ " $\ln$ TOTAL LENGTH ENCODED WITH AN ADD() is: "<<LEN<<endl; cout<<" $\ln$ TOTAL NUMBER OF ADDS = "<<ADDCOUNTER<<endl;
\}//end of add()
\#ifndef NODE_H
\#define NODE_H
class Node $\{$
friend class List;
public:
Node(const int \&);
int getdata();
int NodeIsFlagged(Node *); //checks if a given node has been flagged bool used;
private:
Node * nextPtr;
int data;
\};
Node::Node(const int \& info)
:data(info),nextPtr(0), used(false) \{\}
int Node::getdata()
\{
return data;
\}
\#endif

## //LIST.H

//This is the header file for the list class.
\#ifndef List_H
\#define List_H
\#include"node.h"
class List\{
friend class Node;
public:
List();
void insertAtFront(const int);
bool isEmpty();
void print();
Node * getNewNode(const int \&);
bool setflag(Node *,int); //setflag() takes an encoded offset as //argument \& sets its node to used=true.
int getOffset(Node *);

Node * Fptr();
Node ${ }^{*}$ nPtr(Node*);
private:
Node * firstPtr;
Node * lastPtr;
int count;
\};
\#endif

## //LIST.CPP

```
#include<iostream.h>
#include<cassert>
#include "node.h"
#include "list.h"
#include <stdio.h>
#include <iomanip.h>
const int MAXCOUNT = 5;
List HR[2311];
List::List()
    :firstPtr(0),lastPtr(0), count(0){}
int List::getOffset(Node * ptr)
{
        if(ptr !=0){
                int a = ptr->data;
            return a;
        }
        else
            return -1;
}
```

Node * List: $\mathrm{nPtr}($ Node *ptr)
\{
return ptr->nextPtr;
\}
Node * List::Fptr()
\{
return firstPtr;
\}
bool List::setflag(Node * rptr, int offset)
\{
while(rptr->data != offset)
rptr=rptr->nextPtr;
rptr->used = true;
int nodeoffset $=$ rptr->getdata();
 TRUE"<<endl;
return true; //node is flagged as used.
\}//endofsetflag()

```
void List::insertAtFront(const int value)
{
Node * newPtr = getNewNode(value);
Node * p = firstPtr;
if(isEmpty())
{
    firstPtr = lastPtr = newPtr; count = 1;
}
else
{
    if (count < MAXCOUNT)
    { //while there is still empty nodes in the list
        Node * f = firstPtr;
        if (f!=0)
        while (f !=0) //Insert the offset ONLY if it's not
                //previously inserted i.e. no duplication
            {
        if (f->data == value)
        { /loffset exists in list of HR, don't duplicate
                                break;
            }
        f=f->nextPtr;
        }
        if (f==0)
        {
        newPtr->nextPtr = firstPtr;
        firstPtr = newPtr;
        count++;
        }//endif()
    }//endif()
```

```
else
{
        bool found;
        found = false;
        do //(p->nextPtr != firstPtr)
        {
        if (p->used == true)
        cout<<"\n one used offset found in H}\mp@subsup{H}{R}{\prime\prime}\mathrm{ ;
        p->data = value;
        p->used = false;
        found = true;
    }//endif()
    else
        p = p->nextPtr;
}//endwhile()
while ((p != 0) && !found);
if (!found) // none of the offsets has been used
{
    if (firstPtr == lastPtr)
    {
        firstPtr->data = value;
    }
else
{
        Node * current = lastPtr;
        Node * previous;
        while (firstPtr->nextPtr != current)
        {
            previous = firstPtr;
                    while (previous->nextPtr != current)
                        previous = previous->nextPtr;
                    current->data = previous->data;
                    current = previous;
        }//endwhile()
        current->data = firstPtr->data;
        firstPtr->data = value;
    }//endelse
    }//endif(!found)
```

```
}//endElse()
}//endif()
}//endInsertAtFront()
Node * List::getNewNode(const int & value)
{
    Node * ptr = new Node (value);
    assert (ptr != 0);
    return ptr;
}
bool List::isEmpty()
{
    return (firstPtr == 0);
}
void List::print()
{
    Node * Ptr = firstPtr;
    while(Ptr !=0)
    {
        cout<<Ptr->data<<<" ";
            Ptr = Ptr->nextPtr;
        }//endwhile()
}//endprint()
```

```
//VNODE.H
#ifndef VNODE_H
#define VNODE_H
class VNode{
    friend class VList;
public:
        VNode(const int &);
        int getVdata();
        int VNodeIsFlagged(VNode *); //checks if a given node is empty
        bool coded;
private:
        VNode * VnextPtr;
        int Vdata;
};
VNode::VNode(const int & Vinfo)
    :Vdata(Vinfo),VnextPtr(0), coded(false){}
int VNode::getVdata()
{
    return Vdata;
}
#endif
```


## //VLIST.H

//This is the header file for the VList class.
\#ifndef VList_H
\#define VList_H
\#include"Vnode.h"
class VList\{
friend class VNode;
public:
VList();
void VinsertAtFront(const int);
bool VisEmpty();
void Vprint();

VNode * VgetNewNode(const int \&);
bool Vsetflag(VNode *,int); //Vsetflag() takes an encoded offset as $/ /$ argument \& sets its node to used=true.
int SearchHashTable_V(VNode *); //search HV[] for a given footprint int VgetOffset(VNode *);
VNode * VFptr();
VNode $* \operatorname{VnPtr}($ VNode $*) ;$
private:
VNode * VfirstPtr;
VNode * VlastPtr;
int Vcount;
\};
\#endif

```
//VLIST.CPP
#include<iostream.h>
#include<cassert>
#include "Vnode.h"
#include "VList.h"
#include <stdio.h>
#include <iomanip.h>
const int MAXSIZE = 20;
VList HV[2311];
VList::VList()
    :VfirstPtr(0),VlastPtr(0), Vcount(0) {}
int VList::VgetOffset(VNode * Vptr)
{
        if(Vptr != 0){
            int a = Vptr->Vdata;
            return a;
    }
        else
            return -1;
}
VNode * VList::VnPtr(VNode *Vptr)
{
        if(Vptr)
        return Vptr->V VnextPtr;
            else
                return 0;
}
VNode * VList::VFptr()
{
    return VfirstPtr;
bool VList::Vsetflag(VNode * vvptr,int of)
{
    while (vvptr->V Vdata != of)
                            vvptr = vvptr->VnextPtr;
vvptr->coded = true;
int VNODEOFFSET = vvptr->getVdata();
cout<<"\n\n\t FLAG OF VNODEOFFSET '"<<VNODEOFFSET<<"' IS SET
TO TRUE"<<endl;
```

return true; \}//end of Vsetflag()

```
void VList::VinsertAtFront(const int Vvalue)
{
VNode * VnewPtr = VgetNewNode(Vvalue);
VNode * p = VfirstPtr;
if(VisEmpty())
{
VfirstPtr = VlastPtr = VnewPtr;
Vcount = 1;
}
else
{
if (Vcount < MAXSIZE)
{
    VNode * v = VfirstPtr;
        if (v != 0)
            while (v != 0)
            {
                if (v->Vdata == Vvalue)
                {//Offset exists in HVdon't duplicate
                break;
                }
                    v = v->VnextPtr;
            }//endWhile()
        if (v==0)
        {
            VnewPtr->VnextPtr = VfirstPtr;
            VfirstPtr = VnewPtr;
            Vcount++;
            }//endif()
}//endifVcount<MAXSIZE)
else
{
            VNode * p = VfirstPtr;
```

```
            bool found = false;
    do
    {
        if (p->coded == true)
        {
        cout<<"\n ONE USED OFFSET FOUND ON HV[]";
                    p->Vdata = Vvalue;
                    p->coded = false;
                    found = true;
}//endif()
else
                        p = p->VnextPtr;
    }
    while ((p != 0) && !found);
    if (!found) // none of the offsets has been used
    {
        if (VfirstPtr == VlastPtr)
        {
        VfirstPtr-> Vdata = Vvalue;
        }
        else {
                            VNode * current = VlastPtr;
                    VNode * previous;
            while (VfirstPtr->VnextPtr != current)
            {
                previous = VfirstPtr;
                while (previous->VnextPtr != current)
                    previous = previous->VnextPtr;
                current->Vdata = previous-> Vdata;
                current = previous;
        }//endwhile()
        current->Vdata = VfirstPtr->V data;
        VfirstPtr->Vdata = Vvalue;
}//endElse()
    } //endif(!found)
}//endElse()
```

\}//endif()

## \}//endVInsertAtFront()

```
VNode * VList::VgetNewNode(const int & Vvalue)
{
    VNode * Vptr = new VNode (Vvalue);
    assert (Vptr != 0);
    return Vptr;
}
```

bool VList::VisEmpty()
\{
return VfirstPtr $=0$;
\}
void VList::Vprint()
\{
VNode * VPtr = VfirstPtr;
while(VPtr ! = 0)
\{
cout<<<VPtr->Vdata<<" ";
VPtr $=$ VPtr $->$ VnextPtr;
\}//endWhile()
\}//endVprint()
//DECLARATIONS.H
//This file includes all the declarations of the variables, functions and structures used //in the code.
\#include <iostream.h>
\#include $<$ fstream.h>
\#include <iomanip.h>.
\#include <stdlib.h>
\#include <string.h>
\#include <math.h>
\#include <stdio.h>
\#include <limits.h>
int $\mathrm{p}=3$; //length of the seed.
int TOTALLEN $=0 ; \quad / /$ total length of the adds encoded
const int LISTSIZE $=2311$;
const int SIZE $=100000$;
struct Seed \{
char substring[2000];
\};
struct VerSeed\{
char VerSubstring[2000];
\};
struct ExtendMatch \{
char Rlongest[2];
\};
struct ExtendMatch2 \{
char Vlongest[2];
\};
/*

## THE FUNCTIONS

*/
void proceed(ifstream, ifstream, List[LISTSIZE], VList[LISTSIZE], Seed, VerSeed,int, int, int);
//The following functions encode a string as an $\operatorname{Add}()$ or Copy() command.
void Encode(Node *,VNode *, ifstream, ifstream, List[LISTSIZE],
VList[LISTSIZE], Seed, VerSeed,int, int, int, int, int, int, int);
void outputline(ostream\&, Seed); //outputs a reference string
void outputline2(ostream\&, VerSeed); //outputs a version string
unsigned long footprint(Seed, int, int); //footprint() function for R unsigned long footprint2(VerSeed, int, int); //footprint() function for V int CompareSeeds(Seed, VerSeed); // compare 2 seeds both files

```
void COPY (char *, int, int); //copy a string
void ADD(VerSeed,int,int); //add a string
```

/*
THE VARIABLES
*/
/*
Variables of type Struct()
*/

Seed current, indexedseed, Rseed;
VerSeed versionstring, vstring, indexedverseed, Vseed;
ExtendMatch stretch;
ExtendMatch2 grow;

1*

## POINTERS

*/
Node * Rptr;
Node * RRptr;
Node * longestRptr;
Node * bestRptr;
Node * Tptr;
Node * Sptr;
VNode * Vptr;
VNode * VVptr;
VNode * longestVptr;
VNode * bestVptr;
VNode * Uptr;
VNode * Zptr;
int vs $=0, \mathrm{rs}=0 ;$
//initial offset $=0$ in the Version file
unsigned long F ; //footprint of a seed in R
unsigned long Fv; //footprint of a seed in V
//int $\mathrm{Fr}=0$; //footprint stored in HR[]
//int $\mathrm{FFv}=0$;
//footprint stored in HV[]
//int Rsearchresult $=0 ; \quad / /$ the value returned by function
SearchHashTable_R(): either an 1 or -1
//int Vsearchresult $=0 ; \quad / /$ the value returned by function
SearchHashTable_V(): either an 1 or -1
//the following arrays will temporarily hold each string currently being manipulated
char matchREF[3];
char matchVER[3];
char matchREF2[3];
char matchVER2[3];
//the following arrays will hold the longest matching substrings to be copied char REFlongestmatch[SIZE];
char VERlongestmatch[SIZE];
char REFlongestmatch2[SIZE];
char VERlongestmatch2[SIZE];
char REFlong[SIZE];
char VERlong[SIZE];
char REFlong2[SIZE];
char tempstring[SIZE];
char returned[SIZE];
char STRING_TO_ADD[3];
//temporary storage for the strings to
be Encoded with an ADD() char ADDED_STRINGS[1000]; //

PERMANENT STORAGE of ALL
the Strings Encoded with an ADD()
int cmp;
long $\mathrm{rc}=0, \mathrm{rcc}=0, \mathrm{rcmatch}=0$; // offset of the first character of the substring in R long $\mathrm{rm}=0$; //the starting offset of a matching substring in R
long $\mathrm{vc}=0, \mathrm{vcc}=0, \mathrm{vcmatch}=0 ; / /$ offset of the first character of the current string in $V$
long $\mathrm{vm}=0$; // starting offset of a matching substring in V
int $\ln =0, \ln 2=0 ; \quad / /$ length of the longest matching string
int len $=0$, leng $=0$, len $2=0 ; \quad / /$ holds the length of the longest matching string int longueur $=0$;
int lngth $=0$;
int bestoffset $\mathrm{R}=0$;
int bestoffset $V=0$;
int matching $V=0$;
int matchingR $=0$;
int $\mathrm{ADDCOUNTER}=0$;
int COPYCOUNTER $=0$;
/*
$\qquad$

## END OF DECLARATIONS

*/

